

NAME \_\_\_\_\_

### Gravity and constant acceleration

If an object is thrown up and falls down then:

Time up = Time down = half entire time.

Dis at bottom is 0.

V at top = 0

$V_i$  up =  $-V_f$  down

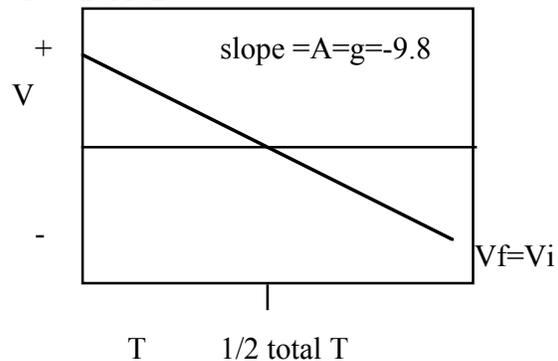
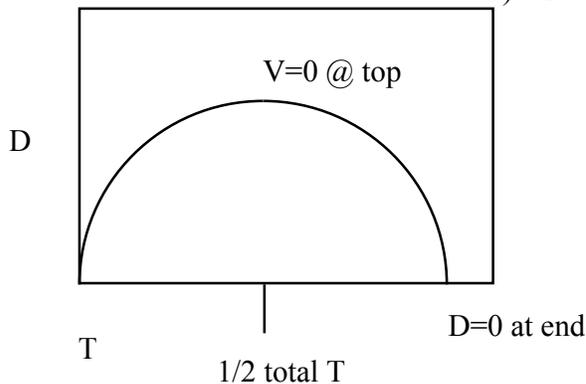
$$1) D = \frac{(V_i + V_f) * T}{2}$$

$$3) V_f = V_i + A * T$$

$$2) V_{avg} = \frac{(V_i + V_f)}{2}$$

$$4) D = V_i * T + \frac{1}{2} * A * T^2$$

$$5) V_f^2 = V_i^2 + 2 * A * D$$



G Problems:

1) If I throw up a baseball straight into the air at 8 m/s, (assume  $g = -9.8$ )

a) what is its velocity at the top of its journey?

**$V_f = 0$  at top**

b) How much time does it take to go all the way up?

**$V_f = 0, V_i = 8, A = -9.8$**

**$V_f = V_i + AT \quad 0 = 8 - 9.8T \quad 9.8T = 8 \quad T = 8/9.8 = .81632 \text{ seconds}$**

c) How much time does it take to go down?

**Same amount of time  $T = .81632 \text{ seconds}$**

**Total time up and down,  $D=0, V_i=8, A=-9.8$**

**$D = V_i T + \frac{1}{2} * A T^2$**

**$0 = 8T + \frac{1}{2} * -9.8 T^2$**

**$0 = 8 - 4.9T \quad T = 8/4.9 = 1.632 \text{ seconds for whole trip, } \frac{1}{2} = .81632 \text{ seconds}$**

d) What is its final velocity when it hits the ground?

**$V_f = V_i + AT$**

**$V_f = 8 + (-9.8)(1.632) = 8 - 16 = -8 \text{ m/s}$**

$$\begin{aligned} \text{Or } V_f^2 &= V_i^2 + 2AD \\ &= 8^2 + 2(-9.8)(0) \\ \text{so } V_f &= \pm 8 \text{ m/s} \end{aligned}$$

2) A pebble is dropped down a well and hits the ground 1.5 seconds later. What is the displacement from the edge of the well to the water surface?

$$V_i = 0 \text{ (dropped)}$$

$$A = -9.8$$

$$T = 1.5$$

$$D = ???$$

$$D = V_i T + \frac{1}{2} AT^2$$

$$D = 0 * 1.5 + \frac{1}{2} * -9.8 * 1.5^2$$

$$D = -4.9 * 2.25 = -11.025 \text{ m (downwards)}$$

3) A gymnast is practicing a dismount from the high bar that is 4 meters off the ground, and swings up with a velocity of + 4 m/s. How fast will she be going when she hits the ground?

$$V_i = 4, A = -9.8, D = -4 \text{ m (because up is positive, and she's ending up below the start)}$$

$$V_f^2 = V_i^2 + 2AD$$

$$V_f^2 = 4^2 + 2(-9.8)(-4)$$

$$V_f^2 = 16 + 78.4 = 94.4$$

$$\text{so } V_f = \pm 9.7 \text{ m/s or } -9.7 \text{ m/s downwards}$$

4) I drop a meterstick and catch it at the 32 cm mark. What is my reaction time?

$$V_i = 0, A = -9.8, D = -32 \text{ cm} = -.32 \text{ m}, T = ???$$

$$D = \frac{1}{2} g T^2$$

$$.32 = \frac{1}{2} * 9.8 * T^2$$

$$T = \text{SQRT} ( 2 * .32 / 9.8 ) = \text{SQRT} (.0653) = .256 \text{ seconds}$$

5) I jump straight up and hit the ground 3 seconds later.

How fast was I going when I started?

$$V_i = ????, T = 3, D = 0 \text{ (hit ground)}, A = -9.8$$

$$D = V_i T + \frac{1}{2} AT^2$$

$$0 = V_i * 3 + \frac{1}{2} * -9.8 * 3^2$$

$$0 = 3V_i - 4.9 * 9$$

$$44.1 = 3V_i \quad V_i = 14.7 \text{ m/s}, V_f = -14.7 \text{ m/s}$$

$$\text{or at top of journey, } V_f = 0, T = 1/2 \text{ total } t = 1.5, A = -9.8$$

$$V_f = V_i + A T \quad 0 = V_i - 9.8 * 1.5 \quad V_i = 14.7 \text{ m/s}$$

What is the total DISTANCE I traveled (not displacement)

**Total distance equals distance up plus distance down, or twice distance down.**

**Starting at top  $T=1.5$ ,  $V_i=0$ ,  $A = -9.8$ ,  $D=??$**

$$D=ViT + \frac{1}{2} * AT^2$$

$$D=0T + \frac{1}{2} * -9.8 * 1.5^2$$

$$D=11.025m \text{ so total distance} = 22.05 m$$

**Or use #5 for first half of journey,  $V_i=14.7$ ,  $V_f=0$ ,  $A = -9.8$ ,  $T=1.5$**

$$0^2=14.7^2 + 2(-9.8)D$$

$$0^2= 216.09+ - 19.6D$$

$$216.09=19.6D \quad D=11.025m \text{ up, so total } D \text{ is } 2*11.025 = 22.05 m$$

6) A robot probe drops a camera off the rim of a 24 km deep crater on Mars, where the free fall acceleration is  $-3.7 \text{ m/s}^2$ .

Find the time required for the camera to reach the crater floor and the velocity with which it hits.

**$D = -24 \text{ km} = -24000 \text{ m}$ ,  $V_i=0$ ,  $A = -3.7$   $T=???$**

$$D=ViT + \frac{1}{2} * AT^2$$

$$-24000=0T + \frac{1}{2} * -3.7 * T^2$$

$$-24000 = -1.85 T^2$$

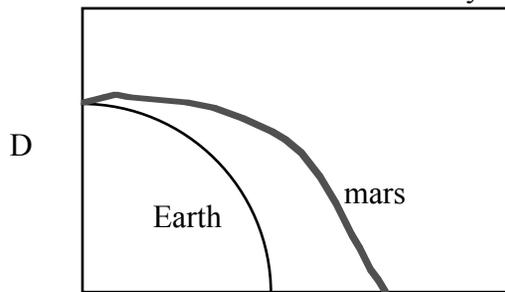
$$T^2 = 24000/1.85 \text{ so } T = 113 \text{ seconds or } 1.89 \text{ minutes}$$

$$V_f^2=0^2 + 2(-3.7)(-24000)$$

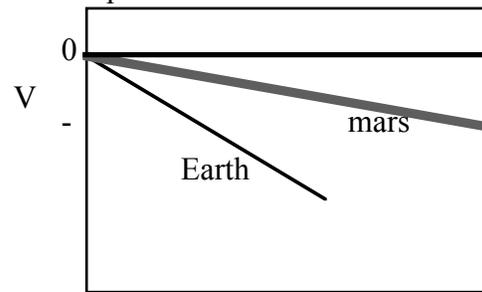
$$V_f^2=177600$$

$$V_f=421.4 \text{ m/s}$$

Sketch the distance time and velocity time graph as compared to Earth.



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